droxide or $t$-butoxide- $t$-butyl alcohol involved a significant degree of competition between phenyl and allyl as leaving groups. Most important, however, the hydrocarbon which did result from the desired phos-phorus-allyl cleavage proved to be a $3: 1$ isomeric mixture of XI and XII, thus making this procedure unattractive from a synthetic standpoint. The carbon-


XI


XII
phosphorus bond can also be cleaved reductively by $\mathrm{LiAlH}_{4},{ }^{15}$ electrolysis, ${ }^{16}$ zinc-acid, and lithium-amine. ${ }^{17}$ However, treatment of X with $\mathrm{LiAlH}_{4}$ led exclusively to Sn $2^{\prime}$ product XII. The method which demonstrated the greatest promise was the reported reduction with lithium in ethylamine at $-76^{\circ}$, giving a $43 \%$ yield of the desired hydrocarbon XI. Since the low yield could be ascribed to competitive cleavage of phenyl and allyl (as observed for the hydroxide-water cleavages), or phenyl reduction by lithium-ethylamine, we used the tri- $n$-butylphosphonium salts, for which no such ambiguity should exist, in order to reach a successful conclusion (vide supra).

More highly hindered allylic systems such as the cyclopentenyl alcohol XIII ${ }^{18}$ may also be coupled with, for example, trans-farnesol (III) to give XIV ( $63 \%$ ). ${ }^{19}$


XIII


XIV

Coupling of XIII with the functionalized trans-farnesol trisnor acetal XV ${ }^{10}$ to give acetal $\mathrm{XVI}^{20}$ is further indi-



XV


XVI
cation of the general applicability of this sequence, as is the alkylation of the intermediate ylides by alkyl iodides and bromides. The generality of this method for the preparation of pure 1,5 -dienes and the preparation of 1,4-dienes by lithium aluminum hydride reduction of

[^0]substituted allyl phosphonium salts portend some breadth of synthetic utility.

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## Barriers in Ethyl Cations ${ }^{1}$

Sir:
Because of geometrical restrictions, many carbonium ions cannot achieve the preferred planar structure. ${ }^{2,3}$ Bridgehead cations are examples of such nonplanar carbonium ions. ${ }^{4}$ While it would be desirable to perform rigorous and reliable molecular orbital calculations on these ions, such calculations are impossible at present because of the large size of such systems. For finding the energies associated with nonplanarity and with torsional interactions in nonplanar ions, the ethyl cation, the simplest ion for which torsional barriers are possible, is an obvious model. In addition, it is the simplest ion in which classical and bridged structures may be compared.

Several calculations, at various levels of sophistication, have been reported for the ethyl cation. ${ }^{3,5-8}$ However, the effects of extensive variation of geometry have not generally been considered, especially by the most refined methods. In this communication, we wish to report the results of two sets of ab initio calculations on ethyl cations which are relevant to both the rotational barrier in classical structures (planar and tetrahedral $\mathrm{CH}_{2}{ }^{+}$) and the bridge barrier for the interconversion by 1,2-hydride shift of equivalent classical structures.

The first set of calculations used the same basis set as ref 3 , with two scaled s-type groups of gaussian orbitals on each hydrogen. In general, threefold rotational barriers computed by this method are accurate to within $\pm 0.4 \mathrm{kcal} / \mathrm{mol} .^{9}$ Five geometries were considered, and the energies are presented in Table I. For each calculation the methyl group was tetrahedral, with a CH bond length assumed to be $1.096 \AA$. The CH bond length in the trigonal $\mathrm{CH}_{2}{ }^{+}$group was kept at
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III

Figure 1. Geometries of classical and bridged ethyl cations.
$1.084 \AA$, and a constant CC length, $1.48 \AA$, the previous determined energy value, ${ }^{3}$ was used. In calculations 1 and 2 , the methylene center was kept planar. As a model for torsional energies in nonplanar cations, calculations 3,4 , and 5 were carried out with the $\mathrm{CH}_{2}{ }^{+}$ group tetrahedral in staggered, intermediate (smallest two dihedral HCCH angles $=30^{\circ}$ ), and eclipsed rotational conformations.
These results suggest that, if the $\mathrm{CH}_{3}$ and $\mathrm{CH}_{2}{ }^{+}$ groups are held in tetrahedral and planar geometries, respectively, the sixfold rotational barrier is effectively zero. ${ }^{3,7}$ However, when the $\mathrm{CH}_{2}{ }^{+}$group is made rigidly tetrahedral, the sixfold barrier becomes threefold, and the barrier height rises to $2.8 \mathrm{kcal} / \mathrm{mol}$, approximately the value for ethane. ${ }^{9,10}$ Interestingly, the energy required to distort the methyl and ethyl cations out of the $\mathrm{RCH}_{2}+$ plane is very similar, despite the difference in the attractive and repulsive energy changes for each system (Table I). This similarity in distortion energy suggests that it may be possible to use the methyl and ethyl cations as fairly reliable models for the behavior of more highly substituted carbonium ions.
The second series of molecular orbital calculations made use of the recently developed STO-3G minimal basis set. ${ }^{11}$ Standard molecular $\zeta$ values were used. ${ }^{11}$ The results of such calculations are known to parallel closely those based on a minimal Slater-type orbital set (STO). In STO-3G, each STO is replaced by a least-squares-fitted sum of three gaussian functions. Also, the computations are sufficiently rapid that complete minimization of the energy with respect to several geometrical parameters is possible. Previous studies have shown that this basis set leads to good agreement with experimental geometries. ${ }^{12}$

In Table II, we present energies found for the three structures illustrated in Figure 1. In calculations 6 and 7, the bond angles were held at tetrahedral $\left(\mathrm{CH}_{3}\right)$ and trigonal values $\left(\mathrm{CH}_{2}+\right)$ and the bond lengths optimized. This leads to $r_{\mathrm{CH}}\left(\mathrm{CH}_{3}\right)=1.095 \AA, r_{\mathrm{CH}}\left(\mathrm{CH}_{2}\right)=1.115$ $\AA$, and $r_{\mathrm{CC}}=1.495 \AA$ for structures I and II. The very small difference between the two energies confirms the

[^1]Table I. Ab Initio Energies for Planar and Tetrahedral Structures ${ }^{a}$

| Calculation | Geometry | $\Delta V_{\mathrm{att}}{ }^{\text {c }}$ | $\Delta V_{\text {rep }}{ }^{\text {d }}$ | $\Delta E$ |
| :---: | :---: | :---: | :---: | :---: |
| Ethyl Cation ${ }^{\text {b }}$ |  |  |  |  |
| 1 | Structure I, $\mathrm{CH}_{2}$ planar | 0.0 | 0.0 | 0.0 |
| 2 | Structure II, $\mathrm{CH}_{2}{ }^{+}$planar | $-0.1{ }^{e}$ | $0.1{ }^{\text {e }}$ | $0.0{ }^{\text {e }}$ |
| 3 | $\begin{aligned} & \mathrm{CH}_{2}+\text { tetrahedral }, \\ & \text { staggered } \\ & \left(\phi=60^{\circ}\right)^{\prime} \end{aligned}$ | $-263.4^{e}$ | $296.1^{\circ}$ | $32.6{ }^{\circ}$ |
| 4 | $\mathrm{CH}_{2}+$ tetrahedral, intermediate $\left(\phi=30^{\circ}\right) f$ | $0.9 g$ | 0.58 | 1.48 |
| 5 | $\mathrm{CH}_{2}{ }^{+}$tetrahedral, eclipsed $\left(\phi=0^{\circ}\right)^{f}$ | $2.3{ }^{\circ}$ | 0.50 | 2.88 |
| Methyl Cation |  |  |  |  |
|  | Planar | 0.0 | 0.0 | 0.0 |
|  | Tetrahedral | $-0.2^{h}$ | $32.7^{\text {h }}$ | $32.5{ }^{\text {h }}$ |

${ }^{a}$ All energies in $\mathrm{kcal} / \mathrm{mol}$. ${ }^{b}$ See Figure 1 and text. Tetrahedral geometry for $\mathrm{CH}_{3}$ assumed. ${ }^{c}$ Sum of nuclear-elestron at tractions. dSum of positive (repulsive) energies: electron-electron and nuclear-nuclear interactions and electron kinetic energies. ${ }^{e}$ Relative to the energy of the planar form of $I$ (calculation 1) -78.24224 hartrees $=-2128.971 \mathrm{eV}(1$ hartree $=27.210 \mathrm{eV}=$ $627.502 \mathrm{kcal} / \mathrm{mol}$ ). ${ }^{\prime} \mathrm{HCCH}$ torsional angles. ${ }^{a}$ Relative to the energy for the tetrahedral, staggered ion (calculation 3). ${ }^{h}$ Relative to the energy of the planar form; total energies: -39.20731 hartrees $=-1066.831 \mathrm{eV}$.
earlier conclusion that rigid rotation gives effectively a zero sixfold barrier. ${ }^{3}$

Table II. STO-3G ${ }^{11}$ Energies for Geometrically Optimized Ethyl Cation Structures

| Calcula- <br> tion | Geometry ${ }^{a}$ | $E^{b}$ | $\Delta E^{c}$ |
| :---: | :---: | :---: | :---: |
| 6 | Structure I, <br> lengths optimized <br>  <br> $d$ | -77.406062 | 1.25 |
| 7 | Structure II, <br> lengths optimized <br>  <br> d | -77.406059 | 1.25 |
| 8 | Structure I, <br> full optimization | -77.408055 | 0.22 |
| 9 | Structure II, <br> full optimization | -77.407703 | 11.42 |

${ }^{a}$ See Figure 1 and text. ${ }^{b}$ Total energies in hartrees. ${ }^{c}$ Energies in $\mathrm{kcal} / \mathrm{mol}$ relative to calculation 8 (the predicted equilibrium geometry). ${ }^{d}$ Tetrahedral $\mathrm{CH}_{3}$ and trigonal $\mathrm{CH}_{2}{ }^{+}$assumed.

In calculations 8 and 9 , all geometrical parameters in structures I and II were varied, the only restriction being the retention of a single reflection plane as shown. As a result of change of bond angles away from the previously fixed values, the energy of structure I is lowered by $1.25 \mathrm{kcal} / \mathrm{mol}$ and that of structure II by $1.03 \mathrm{kcal} /$ mol. Thus, if the bond angles are allowed to change during internal rotation about the $\mathrm{C}-\mathrm{C}$ bond, a sixfold barrier of $0.22 \mathrm{kcal} / \mathrm{mol}$ is predicted, structure I having the lowest energy.

Full details of the predicted STO-3G equilibrium geometry of this and other small hydrocarbons will be presented in a future publication. One feature of interest in $\mathrm{C}_{2} \mathrm{H}_{5}^{+}$is that the angle $\mathrm{C}_{1} \mathrm{C}_{2} \mathrm{H}_{3}$ in structure I is reduced to $102.2^{\circ}$, which may be interpreted as a partial approach toward a bridged protonated-ethylene struc-
ture. However, the $\mathrm{CH}_{2}{ }^{+}$plane for structure I is displaced $2.9^{\circ}$ upward from the $\mathrm{C}-\mathrm{C}$ line toward $\mathrm{H}_{3}$. This corresponds to a small distortion toward a staggered ethane type of geometry.

Calculation 10 refers to the symmetrically bridged structure III which is found to be $11.4 \mathrm{kcal} / \mathrm{mol}$ less stable than the most stable classical form (I). This is close to the $a b$ initio value previously calculated ( 9.0 $\mathrm{kcal} / \mathrm{mol}$, without full optimization), ${ }^{3}$ and in very good agreement with Pfeiffer and Jewett's value ( $12.1 \mathrm{kcal} /$ mol, with partial minimization). ${ }^{8}$ The $\mathrm{CH}_{2}$ groups are bent away from the bridging hydrogen $\left(\mathrm{H}_{3}\right)$, and $2.5^{\circ}$ from the $\mathrm{C}-\mathrm{C}$ line as shown (III). The perpendicular distance of the bridging proton from the $\mathrm{C}-\mathrm{C}$ bond is $1.15 \AA$.
To determine whether the bridged structure III is a saddle point on the potential surface (transition state) or a local minimum (intermediate) in the degenerate rearrangement of one classical ethyl cation to another, a computation was carried out in which $\mathrm{H}_{3}$ was moved $0.05 \AA$ parallel to the $\mathrm{C}-\mathrm{C}$ bond and the planes $\mathrm{H}_{4} \mathrm{C}_{2} \mathrm{H}_{5}$ and $\mathrm{H}_{1} \mathrm{C}_{1} \mathrm{H}_{2}$ were rotated counterclockwise by $1^{\circ}$. This lead to an energy lowering of $40 \mathrm{cal} / \mathrm{mol}$, indicating that III is a transition state and not a metastable species (intermediate). Thus, these calculations predict a gasphase activation barrier of $11.4 \mathrm{kcal} / \mathrm{mol}$ for 1,2 -hydride shifts in the ethyl cation. ${ }^{13}$

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## Activated Complex for Hydrogen Migration in the Ethyl Cation. Ab Initio Calculations

Sir:
We wish to report the results of $a b$ initio LCAO-MO SCF calculations concerning the structure of the ethyl cation. ${ }^{1}$ The results of the calculations bear on two related problems of experimental and theoretical interest. First, we are concerned with the relative stabilities of open or "classical" and hydrogen-bridged or "nonclassical" ethyl cations. Second, we wish to ex-

[^2]amine whether a hydrogen-bridged structure is best described as an activated complex or an intermediate for 1,2 hydride migration in the ethyl cation. Of course these calcuations apply only to the gas phase and solvation effects may alter the equilibrium geometry and structure of carbonium ions in solution.

Previous semiempirical calculations for $\mathrm{C}_{2} \mathrm{H}_{5}{ }^{+}$have given conflicting predictions concerning the structure of the ethyl cation: some reports indicate the bridged structure to be more stable ${ }^{2}$ while other reports find the open structure as the more stable conformation. ${ }^{3} A b$ initio calculations including the present work indicate that the bridged structure is less stable than the classical conformation. ${ }^{1,26,4}$ In Table I we give the energies for

Table I. Energies for Bridged and Classical Structures

| Structure $^{a}$ | $E^{b}$ | $\Delta E^{c}$ |
| :---: | :---: | ---: |
| A | -78.22466 | 12.43 |
| B | -78.22519 | 12.10 |
| C | -78.22920 | 9.58 |
| D | -78.24446 |  |

${ }^{a}$ For a description of the structures see Figure 1 and text. ${ }^{b}$ Total energies in hartrees. ${ }^{c}$ Energies in $\mathrm{kcal} / \mathrm{mol}$ relative to structure D.
the bridged and classical structures shown in Figure 1. The basis set for these calculations consists of gaussian lobe functions with Whitten's exponents and coefficients for each function. ${ }^{5}$ The $\mathrm{H}(1 \mathrm{~s})$ function is represented by a linear combination of five gaussian functions. All of the calculations reported here were obtained with the five-term hydrogen function split into two parts which were then individually subject to linear minimization by the SCF procedure. A basis set of this quality has had excellent success in yielding molecular geometries in close agreement with experiment. ${ }^{6}$ We have examined a large number of conformations of $\mathrm{C}_{2} \mathrm{H}_{5}+$ in an effort to find relative energies and optimal geometries for the open and bridged forms. In addition we wished to understand the bonding environments in these conformations and have performed population analyses on each of the conformations studied. The details of the energy terms of the numerous conformations studied as well as population analyses for these conformations will be presented in a full paper. We describe here points of immediate interest.

For the open or classical ethyl cation we first consider a structure with the $\mathrm{CH}_{3}$ group tetrahedral with $r_{\mathrm{CH}}=1.091 \AA$, the $\mathrm{CH}_{2}$ group trigonal with $r_{\mathrm{CH}}=$ $1.086 \AA$, and a plane of symmetry through one of the $\mathrm{CH}_{3}$ hydrogens and the CC bond. Energy minimization with respect to the CC bond length yields $r_{\mathrm{CC}}=$ $1.51 \AA$. The choice of a planar cationic center has previously been shown to yield the equilibrium confor-

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    (20) Identical with an authentic sample prepared independently. $\mathrm{Nmr}\left(\mathrm{CCl}_{4}\right) \delta 5.0-5.3$ ( $3, \mathrm{broad}$ ), $4.75(1, \mathrm{t}, J=6 \mathrm{~Hz}), 3.78-3.95(4, \mathrm{~m})$, 2.4-2.6 (1, broad), $1.8-2.4$ (14, broad), 1.56 ( 9 , broad s), 0.92 ( $3, \mathrm{~d}$, $J=7 \mathrm{~Hz}), 0.66(3, \mathrm{~d}, J=7 \mathrm{~Hz})$.

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